



# AS Level Physics

Chapter 2 – Mechanics

2.9.1 Newton's Laws of Motion and Momentum

Notes

## NEWTON'S THREE LAWS OF MOTION

### Newton's 1<sup>st</sup> Law of Motion

Newton's 1<sup>st</sup> Law of motion states:

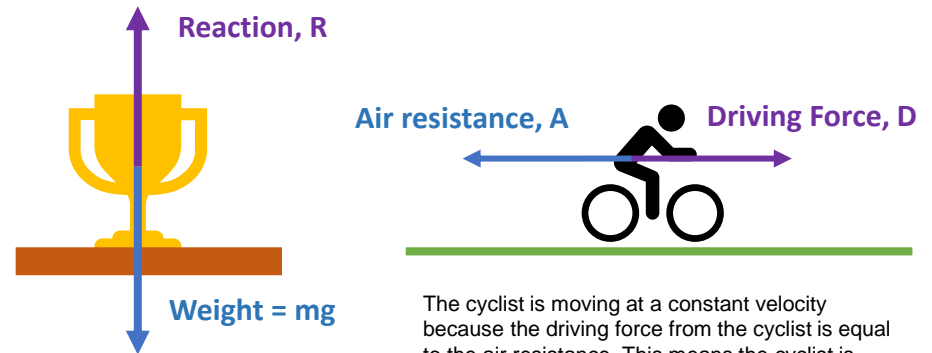
**“an object will remain at rest (or stationary) or continue to travel with a constant velocity unless acted upon by a resultant force”**

- This means an object will remain still or move with a constant speed, in a straight line, in the same direction unless acted upon by a resultant (net) or unbalanced force.
- If an object has a zero resultant force acting on it, the object is said to be at rest or moves with a constant velocity (or uniform motion).
- Zero resultant force means the combined effect of all the forces acting on the object is zero.
- Therefore FORCE is something that tries to change the state of rest or uniform motion of an object, either through constant or 'field' action (i.e. electric, gravity or magnetic fields).

## NEWTON'S THREE LAWS OF MOTION

### Newton's 1<sup>st</sup> Law of Motion

Examples:



The trophy is stationary or at rest because the reaction force is equal to the weight of the object. This means the forces are balanced and the resultant force is zero. The trophy will only move when a resultant force acts on it, i.e. if someone comes and pushes the trophy over.

The cyclist is moving at a constant velocity because the driving force from the cyclist is equal to the air resistance. This means the cyclist is moving in the same direction with a constant speed. Therefore the forces are balanced and the resultant force is zero. The cyclist will continue to move in the same direction with the same speed unless a resultant force acts on him i.e. he chooses to speed up or change direction.

### INERTIA

- It is the natural tendency of every object to resist the change in their state of motion. If they are at rest, they want to stay at rest and if they're moving with a constant velocity they would want to continue to do so. This tendency of objects is called INERTIA.
- Therefore, INERTIA is a resistance to a change in motion (both speed and direction). Unless an external force causes a change, objects want to remain at rest or in motion.
- All objects have inertia and the greater the mass of an object, the greater is its inertia. This results in applying a greater resultant force in order to change the motion of the object.
- For example it is more difficult to change the motion of a box full of bricks compared to changing the motion of an empty box because the box full of bricks weighs a lot more.

## NEWTON'S THREE LAWS OF MOTION

### Newton's 2<sup>nd</sup> Law of Motion

Newton's 2<sup>nd</sup> Law of motion states:

**“The rate of change of momentum of an object is directly proportional to the applied resultant force and occurs in the direction of the resultant force”**

- In other words, the resultant force is proportional to the change of momentum per second.
- At GCSE you learn that Newton's 2<sup>nd</sup> law is defined as  $F = ma$  (force = mass x acceleration). At A-level we will look at how this equation is derived from Newton's 2<sup>nd</sup> law in its general form as stated above. But first you need to know what momentum is:

#### Momentum:

The momentum of an object is the product of its mass and velocity.

$$p = m \times v$$

where:

$p$  = Momentum measured in  $kg \text{ ms}^{-1}$ .

$m$  = mass measured in  $kg$ .

$v$  = velocity measured in  $ms^{-1}$ .

Momentum is a vector and therefore has both magnitude and direction. This means momentum to the right can be considered positive and momentum to the left can be negative.



## NEWTON'S THREE LAWS OF MOTION

### Newton's 2<sup>nd</sup> Law of Motion

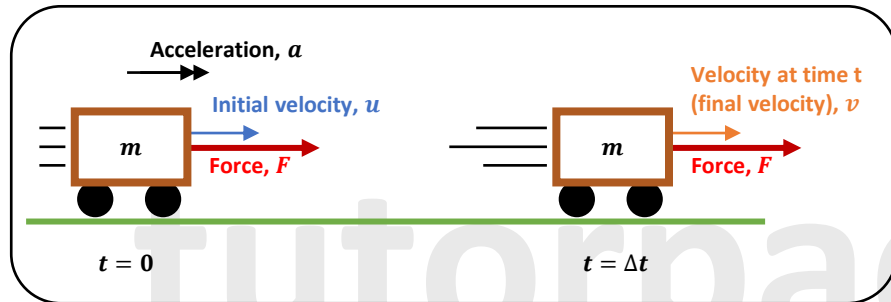
- Note, force acting on an object can cause a change in its momentum. A large force results in a greater rate at which the objects momentum changes.
- E.g. the harder you throw a ball, the greater is its rate of change of momentum and the more difficult it is to catch.



## NEWTON'S THREE LAWS OF MOTION

### Newton's 2<sup>nd</sup> Law of Motion

- Now let's look at how  $F = ma$  is derived from Newton's 2<sup>nd</sup> law.
- Consider an object of a constant **mass ( $m$ )** acted on by a **constant force,  $F$** . This causes the object to move with a **constant acceleration ( $a$ )** causing the velocity to change from a **initial velocity ( $u$ )**, at **time zero ( $t = 0$ )**, to a **final velocity ( $v$ )** in a **time ( $t = \Delta t$ )** without a change of direction.



- The initial momentum of the object:  
 $p_i = mu$
- The final momentum of the object:  
 $p_f = mv$
- Therefore the momentum change:  
 $\Delta p = \text{final momentum} - \text{initial momentum}$   
 $\Delta p = mv - mu$

## NEWTON'S THREE LAWS OF MOTION

### Newton's 2<sup>nd</sup> Law of Motion

- According to Newton's 2<sup>nd</sup> law, the force is proportional to the rate of change of momentum, therefore:

$$F \propto \frac{\text{change of momentum}}{\text{time taken}} = \frac{\Delta p}{\Delta t}$$

$$F = \frac{mv - mu}{\Delta t}$$

$$F = \frac{m(v - u)}{\Delta t}$$

$$\text{Therefore, } F = ma$$

But we know that acceleration is:

$$a = \frac{(v - u)}{\Delta t}$$

And therefore we substitute  $a$  in the equation.

Where  $a = \frac{(v-u)}{\Delta t}$  = the acceleration of the object.

- So from Newton's 2<sup>nd</sup> Law we have confirmed:  
*Resultant force ( $F_R$ )  $\propto$  rate of change of momentum ( $= ma$ )*
- This proportionality relationship can be written as below:  
 $F_R = kma$ , where  $k = \text{constant of proportionality}$
- Typically,  $k$  is made to equal 1 by defining the unit force (1 N) as the amount of force that gives an object, of mass 1 kg, an acceleration of  $1 \text{ ms}^{-2}$ .
- Therefore,  $k = 1$ , gives us  $F = ma$  following from Newton's 2<sup>nd</sup> law.
- Note:  $F = ma$  is only valid so long as the mass of the object is constant.

## NEWTON'S THREE LAWS OF MOTION

### Worked Example 1:

A football of mass  $0.46\text{ kg}$  initially at rest was struck which gave it a velocity of  $25\text{ms}^{-1}$ . The contact time between the foot and the ball was  $15\text{ms}$ .

Calculate:

- The momentum gained by the ball,
- The average force of impact on the ball.

### Solution:

- a) Using: *change of momentum* =  $mv - mu$

$$\text{Momentum gained} = (0.46\text{kg})(25\text{ms}^{-1}) - (0.46\text{kg})(0\text{ms}^{-1})$$

$$\text{Momentum gained} = 11.5\text{ kgms}^{-1}$$

- b) Using:  $F = \frac{\text{change of momentum}}{\text{time taken}} = \frac{\Delta p}{\Delta t} = \frac{mv - mu}{\Delta t}$

$$F = \frac{11.5\text{ kgms}^{-1}}{0.015\text{s}} = 766.67\text{ N}$$

$$\text{Impact force} = 767\text{ N}$$

$$15\text{ms} = 15 \times 10^{-3}\text{s} = 0.015\text{s}$$

Initially the object is at rest therefore initial velocity,  $u = 0\text{ms}^{-1}$

## NEWTON'S THREE LAWS OF MOTION

### Worked Example 2:

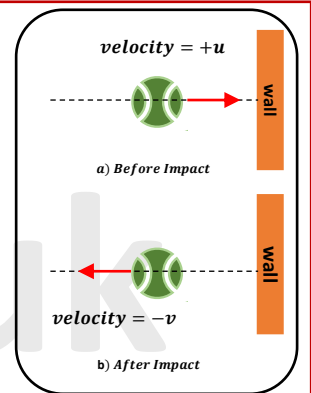
When a ball of mass  $0.30\text{ kg}$  hits a wall at a speed of  $16\text{ms}^{-1}$ , the ball returns in the direction it came from at a speed of  $13\text{ms}^{-1}$ . The contact time was  $0.11\text{s}$ . Calculate:

- The change of momentum of the ball,
- The impact force on the ball.

### Solution:

- a) Using: *change of momentum* =  $mv - mu$

Remember that velocity and momentum are vectors and so they have a magnitude as well as a direction. Suppose the ball hits the wall normally with an initial speed  $u$  and it rebounds at speed  $v$  in the opposite direction. Since its direction of motion reverses on impact, a sign convention is necessary to represent the two directions. Using + for 'towards the wall' and - for 'away from the wall', its *initial momentum* =  $+mu$ , and its *final velocity* =  $-mv$ .



Mass of the ball  $m = 0.30\text{kg}$ , initial velocity  $u = +16\text{ms}^{-1}$ , final velocity  $v = -13\text{ms}^{-1}$ ,

$$\text{Change of momentum} = mv - mu$$

$$\text{change of momentum} = (0.30 \times -13) - (0.30 \times 16)$$

$$\text{change of momentum} = -3.9 - 4.8$$

$$\text{change of momentum} = -8.7\text{ kg m s}^{-1}$$

- b) Using:  $F = \frac{\text{change of momentum}}{\text{time taken}} = \frac{\Delta p}{\Delta t} = \frac{mv - mu}{\Delta t}$

$$F = \frac{-8.7\text{ kgms}^{-1}}{0.11\text{s}}$$

$$F = -79.09\text{ N}$$

The minus sign indicates the direction of the force, i.e. to the left



## NEWTON'S THREE LAWS OF MOTION

### Newton's 2<sup>nd</sup> Law of Motion

#### Weight:

To calculate the **WEIGHT (W)** of an object use:

$$W = mg$$

where:

$W$  = weight measured in *Newtons, N*.

$m$  = mass measured in *kg*.

$g$  = acceleration due to gravity measured in  $\text{N/kg}$  or  $\text{ms}^{-2}$ .

On Earth, acceleration due to gravity is  $g = 9.81 \text{ m s}^{-2}$ .

The formula of weight is a version of  $F = ma$ .

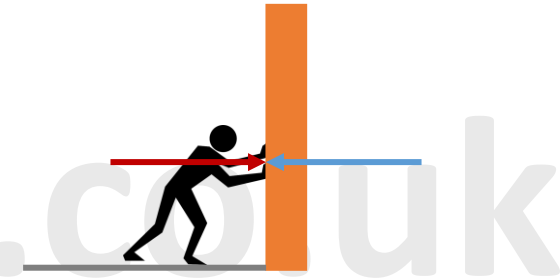
## NEWTON'S THREE LAWS OF MOTION

### Newton's 3<sup>rd</sup> Law of Motion

Newton's 3<sup>rd</sup> Law of motion states:

**“If an object A exerts a Force on object B, then object B exerts an equal but opposite force on object A”**

- For example, if you were to push against a wall, then the wall will push back against you, just as hard. But, as soon as you stop pushing, the wall stops too.



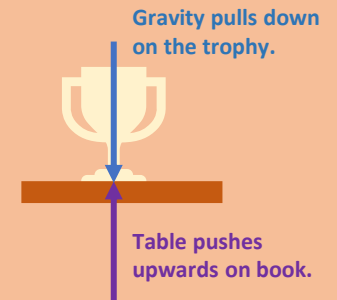
- Newtons 3<sup>rd</sup> Law can occur in all situations and to all types of forces, however the pairs of forces have to be the same type, e.g. both gravitational or both electrical.

This looks like Newton's 3<sup>rd</sup> law....

However it's **NOT**

This is because both forces acting on the trophy are not the same type. These are two separate interactions.

Here, the forces are equal and opposite, resulting in zero acceleration, so this is showing Newton's 1<sup>st</sup> law.

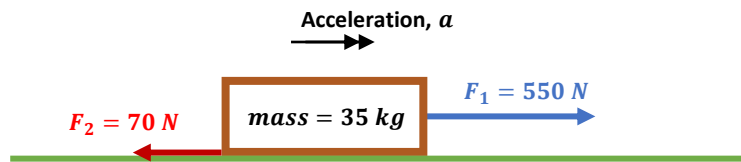


## NEWTONS LAW QUESTIONS

For more force questions please see Module 3 – Forces and motions pack 3.3 Dynamics

### Example 1: Resultant Force

A force of 550 N is used to pull a 35 kg box against a constant frictional force of 70 N as shown below. Calculate the acceleration of the box.



From Newton's 2<sup>nd</sup> law: Resultant force ( $F$ ) = mass ( $m$ ) x acceleration ( $a$ )

$$F_1 - F_2 = ma$$

$$(550 - 70) = 35a$$

$$a = \frac{480}{35}$$

$$a = 13.7 \text{ ms}^{-2} \text{ (1 d.p.)}$$

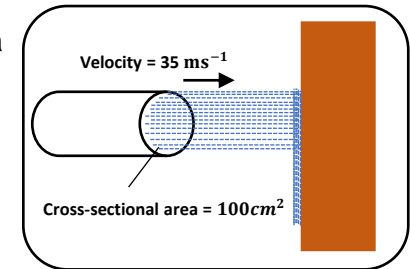
## NEWTONS LAW QUESTIONS

For more force questions please see Module 3 – Forces and motions pack 3.3 Dynamics

### Example 2: Hosepipe

A hosepipe with a cross-sectional area of  $0.01 \text{ m}^2$  ejects a horizontal jet of water at a speed of  $35 \text{ ms}^{-1}$ .

The water hits a wall perpendicularly and flows down the wall without rebounding. Calculate the force exerted on the wall. (Density of water =  $1 \times 10^3 \text{ kg m}^{-3}$ ).



From Newton's 2<sup>nd</sup> law:

Force exerted by the wall on the water = Rate of change of momentum of the water

= mass of water striking wall per second x Velocity change of water

= Volume of water/s x Water density x Velocity change of water

$$= (35 \text{ ms}^{-1} \times 0.01 \text{ m}^2) \times (1 \times 10^3 \text{ kg m}^{-3}) \times (35 \text{ ms}^{-1} - 0 \text{ ms}^{-1})$$

$$= \underline{1.23 \times 10^4 \text{ N}}$$

From Newton's 3<sup>rd</sup> law, there must be an equal and opposite force exerted by the water on the wall.

So, force exerted on the wall =  $1.23 \times 10^4 \text{ N}$



## NEWTONS LAW QUESTIONS

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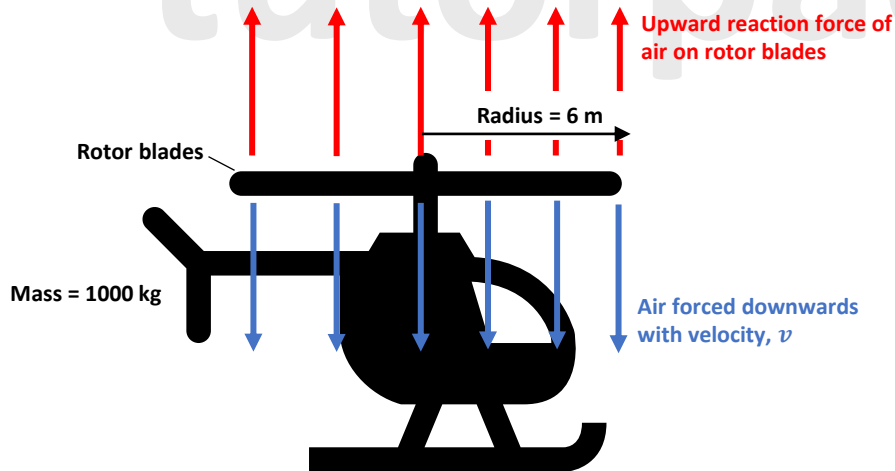
A helicopter can hover in air when the upwards force is equal to its weight (downwards force). This is possible due to Newton's third law. When helicopter blades rotate they force air downwards and an equal and oppositely directed force is exerted by the air on the blades. This principle can be applied to hovering birds and other hovering bodies/objects.

### Example 3: Helicopter

A hovering helicopter of mass 1000 kg. If the length of each rotor blade is 6 m, calculate the velocity of the air forced downwards by the rotor to keep the helicopter hovering in mid-air.

Density of air =  $1.3 \text{ kgm}^{-3}$

Acceleration due to gravity,  $g = 9.81 \text{ ms}^{-2}$



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## NEWTONS LAW QUESTIONS

For more force questions please see Module 3 – Forces and motions pack 3.3 Dynamics

### Example 3: Helicopter

From Newton's 2<sup>nd</sup> law:

Upwards force of air on blades = Rate of change of momentum of air forced down by blades = Helicopter weight

Helicopter weight = mass of air forced down per second  $\times$  Velocity change of air being forced down

Helicopter weight = Volume of air forced down per second  $\times$  Density of air  $\times$  Velocity change of air being forced down

$$mg = \pi R^2 v \times \rho \times v$$

$$v^2 = \frac{mg}{\pi R^2 \rho} = \frac{1000 \text{ kg} \times 9.81 \text{ ms}^{-2}}{\pi \times 6^2 \text{ m}^2 \times 1.3 \text{ kgm}^{-3}}$$

$$v^2 = 66.72 \dots$$

$$v = \underline{8.17 \text{ ms}^{-1}}$$

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Please see **'2.9.2 Newton's Law of Motion and Momentum Worked Examples'** pack for exam style questions.

For more revision notes, tutorials and worked examples please visit [www.tutorpacks.co.uk](http://www.tutorpacks.co.uk).

