



# AS Level Physics

Chapter 4 – Materials

4.3.2 Terminal Velocity

Worked Examples

## TERMINAL VELOCITY

### Exam Style Question 1:

a) A student holds a golf ball and a table tennis ball out of an upper window of a tall building. The balls are released at the same time. Both balls have the same size. The golf ball has a greater mass than the table tennis ball. One of the balls reaches a greater terminal velocity.

- i) State and explain the acceleration of the golf ball immediately after it is released.
- ii) By referring to the forces acting on the golf ball, explain what is meant by terminal velocity.
- iii) Explain which of the two balls reaches the greater terminal velocity.

#### Answer:

- i) State and explain the acceleration of the golf ball immediately after it is released.**

The Earth's gravitational pull causes objects to accelerate as they fall. Any object near the surface of the Earth, the acceleration caused by gravity has an approx. value of:

$$g = \text{acceleration of free fall} = 9.81 \text{ ms}^{-2}.$$

If a object is in free fall, the only force acting on the object is gravity; and therefore, acceleration is equal to  $g$ .

Applying this knowledge to the golf ball, the acceleration of the golf ball immediately after it is released is  $9.81 \text{ ms}^{-2}$  because at that point the only force acting on the golf ball is its own weight caused by gravity and the drag force is zero.

## TERMINAL VELOCITY

### Exam Style Question 1:

#### Answer:

- ii) By referring to the forces acting on the golf ball, explain what is meant by terminal velocity.**

Terminal velocity is when the golf ball has reached its maximum velocity, and this is achieved when drag force = weight.

- iii) Explain which of the two balls reaches the greater terminal velocity.**

The golf ball experiences a greater drag force because it has a greater mass compared to the table tennis ball. This greater mass means a greater weight, and so a stronger drag force is required to achieve terminal velocity.

Therefore, the golf ball will accelerate for a longer time in order to reach a higher terminal velocity where the drag force can equal to the golf balls greater weight. As, the golf ball accelerates for a longer time, it achieves a higher velocity.

So, the golf ball has a greater terminal velocity.



## TERMINAL VELOCITY

### Exam Style Question 2:

- a) State two factors that affect the magnitude of the drag force acting on an object falling through air.
- b) Fig 4.1 shows a skydiver of total mass  $75\text{ kg}$  falling vertically towards the ground.



The air resistance, or drag force,  $D$  in newtons ( $N$ ) acting on the skydiver falling through the air is given by the equation:

$$D = 0.3v^2$$

Where  $v$  is the speed in  $ms^{-1}$  of the skydiver.

- i) On Fig. 4.1, draw arrows to represent the weight (labelled  $W$ ) and drag force (labelled  $D$ ).
- ii) Calculate the weight of the skydiver.
- iii) At a particular instant, the speed of the skydiver is  $20\text{ ms}^{-1}$ . Calculate the instantaneous acceleration of the skydiver.
- iv) State the relationship between the forces  $W$  and  $D$  when the skydiver reaches terminal velocity.
- v) Determine the terminal velocity of the skydiver.



## TERMINAL VELOCITY

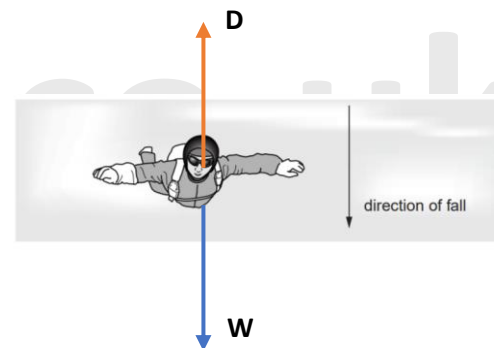
### Exam Style Question 2:

Answer:

a) State two factors that affect the magnitude of the drag force acting on an object falling through air.

- Area (greater the area, greater the drag)
- Speed / velocity (greater the velocity, greater the drag)
- Aerodynamic shape (streamline) (more aerodynamic shaped an object, less frictional forces (drag) affects it)

bi) On Fig. 4.1, draw arrows to represent the weight (labelled  $W$ ) and drag force (labelled  $D$ ).



bii) Calculate the weight of the skydiver.

Use:  $W = mg$

$$W = 75\text{ kg} \times 9.81\text{ ms}^{-2}$$
$$\therefore \text{weight} = 735.75\text{ N} = 736\text{ N}$$

## TERMINAL VELOCITY

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- v) Determine the terminal velocity of the skydiver.

## TERMINAL VELOCITY

### Exam Style Question 2:

Answer:

**biii) At a particular instant, the speed of the skydiver is  $20\text{ ms}^{-1}$ . Calculate the instantaneous acceleration of the skydiver.**

Step 1: Use the formula they gave us to calculate the drag force,  $D$ :

$$D = 0.3v^2$$

$$D = 0.30 \times (20)^2 = 120\text{ N}$$

Step 2: Use  $F = ma$  to find acceleration but first we need to calculate the net (resultant) force:

$$F = W - D = 736 - 120 = 616\text{ N}$$

Step 3: Calculate the acceleration by rearranging  $F = ma$

$$a = \frac{F}{m} = \frac{616\text{ N}}{75\text{ kg}} = 8.2133 = 8.2\text{ ms}^{-2}$$

**biv) State the relationship between the forces  $W$  and  $D$  when the skydiver reaches terminal velocity.**

Terminal velocity is when an object or person reach their maximum velocity, and this is achieved when  $D = W$ .

**bv) Determine the terminal velocity of the skydiver.**

At terminal velocity  $\text{drag} = \text{weight} = 736\text{ N}$ .

We know that drag is:  $D = 0.3v^2$

$$\therefore 736\text{ N} = 0.30 \times v^2$$

Now rearrange the formula to find  $v$  which in turn will give us the terminal velocity:

$$v^2 = \frac{736}{0.3}$$

$$v = \sqrt{\frac{736}{0.3}} = 49.5311 \dots = 49.5\text{ ms}^{-1}$$

So, the terminal velocity of the skydiver is  $49.5\text{ ms}^{-1}$

## TERMINAL VELOCITY

### Exam Style Question 3:

- a) A skydiver jumps from a stationary hot-air balloon several kilometres above the ground.

In terms of acceleration and forces, explain the motion of the skydiver

- i) Immediately after jumping
- ii) At a time before terminal velocity is reached
- iii) At terminal velocity.

b) In the final stage of the fall, the skydiver is falling through air at a constant speed. The skydiver's kinetic energy does not change even though there is a decrease in the gravitational potential energy. State what happens to this loss of gravitational potential energy.

c) Fig 3.1 shows a sketch graph of the variation of the velocity  $v$  of the skydiver with time  $t$ .

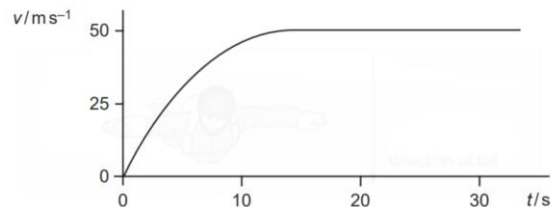


Fig. 3.1

Suggest the changes to the graph of Fig 3.1, if any, for a more massive (heavier) skydiver of the same shape.

## TERMINAL VELOCITY

### Exam Style Question 3:

Answer:

**a) In terms of acceleration and forces, explain the motion of the skydiver**

**i) Immediately after jumping**

Immediately after jumping the only force acting on the skydiver is his own weight and drag is zero. This means he will accelerate with an acceleration equal to  $9.81 \text{ ms}^{-2}$ .

**ii) At a time before terminal velocity is reached**

Before terminal velocity is reached drag increases gradually with speed and the net force decreases. Weight is still greater than drag but acceleration is less than  $9.81 \text{ ms}^{-2}$ .

**iii) At terminal velocity.**

Weight is equal to drag, net force is zero and acceleration is zero. The skydiver has reached his/hers maximum velocity and is falling at a constant velocity.

**b) State what happens to this loss of gravitational potential energy.**

The loss of GPE is transformed to heat/thermal energy.

**c) Suggest the changes to the graph of Fig 3.1, if any, for a more massive (heavier) skydiver of the same shape.**

- 1) The terminal velocity increases.
- 2) Initial gradient/slope is the same/equal to  $9.81 \text{ ms}^{-2}$
- 3) Time taken to reach terminal velocity is longer.

Please see the **'4.3.1 Terminal Velocity notes'** pack  
for revision notes.

For more revision notes, tutorials, worked  
examples and more help visit  
[www.tutorpacks.co.uk](http://www.tutorpacks.co.uk).

