

# **AS Level Physics**

Chapter 3 – Electric Circuits

3.5.1 Series and Parallel Circuit

Notes



© Tutor Packs

@tutorpacks

(O)

## Kirchhoff's Laws

## Kirchhoff's First Law

The total current leaving, any junction in a circuit, is equal to the total current entering the junction.

$$i.e.\sum I_{in}=\sum I_{out}$$

## Kirchhoff's Second Law

Consider the opposite circuit:

Trace the movement of 1 coulomb of charge around the circuit.

Electrical energy is delivered to each coulomb as the charge passes through the first cell with 5 *V* and then through the second cell with 15 *V*. The charge then flows through the 100  $\Omega$  resistor and a filament bulb. In each of those components, the electrical energy is converted to heat in the resistor and heat and light in the bulb.

At A: 5J gained by the charge.

At B: 15J gained by the charge.

Total energy gained = 20J

At C: 10J lost by the charge

At D: 10J lost by the charge

Total energy lost = 20J

tutorpacks.co.uk

© Tutor Packs



## Kirchhoff's Laws

#### Kirchhoff's Second Law

So the charge has lost as much energy as it gained by the time it completes the circuit. This is an example of conservation of energy. So we can conclude:







© Tutor Packs

#### **Resistors in Series**

When resistors are connected in series:

- The current flowing through the resistors is the same.
- The **p.d.** of the supply is **shared** between them.

Consider the following three resistors of resistance  $R_1$ ,  $R_2$  and  $R_3$  connected in series as shown:



Kirchhoff's 1<sup>st</sup> Law states:

The current (I) is constant throughout the circuit. As a result, the current in each resistor is the same.

Kirchhoff's 2<sup>nd</sup> Law states:

The e.m.f. (*E*) is split between the components therefore:

 $E = V_1 + V_2 + V_3$  V = IR, so if I is constant:  $IR_{total} = IR_1 + IR_2 + IR_3$  Cancelling the I's gives: $R_{total} = R_1 + R_2 + R_3$ 

Therefore:

The total resistance  $(R_{total})$ , of any number of resistors, connected in series is given by:

 $R_{total} = R_1 + R_2 + R_3 \dots \dots + R_N$ 

#### tutorpacks.co.uk



Step 1: Sketch a diagram; calculate the combined resistance:

$$R_{total} = R_1 + R_2 = 25\Omega + 15\Omega = 40\Omega$$

Step 2: Calculate the current that flows:

$$I = \frac{V}{R} = \frac{10V}{40\Omega} = 0.25 A$$

Step 3: Calculate the p.d. across each resistor:

Across 20 $\Omega$ :  $V = IR = 0.25A \times 25\Omega = 6.25V$ Across 5 $\Omega$ :  $V = IR = 0.25A \times 15\Omega = 3.75V$ 

tutorpacks.co.uk

## **Resistors in Parallel**

When resistors are connected in parallel:

- The **p.d.** across the resistors is the **same**.
- The current from the supply is shared by the resistors.

Consider the following three resistors of resistance  $R_1$ ,  $R_2$  and  $R_3$  connected in parallel as shown:



tutorpacks.co.uk

# Series and Parallel Circuit

#### **Resistors in Parallel**

Kirchhoff's First Law states:

Because the p.d. is the same across all of the components, each resistors p.d. is equal to *V*.

From the definition of resistance:

$$I = \frac{V}{R}$$

Applying this to equation (1) we get:  $\frac{V}{R_{TOTAL}} = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3}$ 

Cancelling the V's gives:

Therefore:



 $\frac{1}{R_{TOTAL}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$ 

 $\frac{1}{R_{TOTAL}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \dots \dots + \frac{1}{R_N}$ 

For resistors connected in parallel:

- The greatest current is carried by the resistor with the smallest resistance.
- The total resistance of the combination is smaller than the resistor with the smallest resistance in the combination.

tutorpacks.co.uk

## **Special Case for Resistors in Parallel**

When (*N*) resistors with the same resistance (*R*) are connected in parallel, the total resistance ( $R_{total}$ ) is calculated using:

 $R_{total} = \frac{R}{N}$ 

# tutorpa

# Series and Parallel Circuit

10V

25Ω

15Ω

**Resistors in Parallel Worked Example 1** 

A 25  $\Omega$  resistor and a 15  $\Omega$  resistor are connected in parallel with a 10V battery. What current flows from the battery?

Step 1: Calculate the total resistance:



(For resistances connected in parallel, R is always less than the smallest of  $R_1, R_2$ , etc...)

Step 2: Calculate the current from the combined resistance and the p.d.:

$$I = \frac{V}{R} = \frac{10 V}{9.375 \,\Omega} = 1.0666 \dots A$$

I = 1.07 A

tutorpacks.co.uk

tutorpacks.co.uk

© Tutor Packs

18V

7.5Ω

10Ω

6Ω

 $R_A$ 

5Ω

Y

## **Resistors in Series and Parallel Worked Example**

A battery of e.m.f. 18V and negligible internal resistance is connected in a circuit as shown opposite:

- a) Show that the group of resistors between X and Y could be replaced with a single resistor of resistance  $7.5\Omega$ .
- b) If  $R_A = 25\Omega$ :

i) Determine the potential difference across  $R_A$ ,

ii) Calculate the current in the  $7.5\Omega$  resistor.



**Step 1:** First calculate the combined resistance of the resistors in parallel (7.5  $\Omega$ , 10  $\Omega$  and 6  $\Omega$ ):

Χ

$$\frac{1}{R_{total}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} = \frac{1}{7.5} + \frac{1}{10} + \frac{1}{6} = \frac{2}{5}$$
$$\frac{1}{R_{total}} = \frac{2}{5}$$
$$R_{total} = \frac{1}{\left(\frac{2}{5}\right)} = 2.5 \,\Omega$$

**Step 2:** Now that you have calculated the total resistance of the resistors in parallel you can re-draw the circuit to make it easier to visualise:



$$R_{total} = R_1 + R_2 = 2.5\Omega + 10\Omega$$
$$R_{total} = 7.5\Omega$$

#### tutorpacks.co.uk



#### **Resistors in Parallel Worked Example 1**

#### b) Calculate the p.d. across $R_A$ :

To calculate the p.d. we need to use V = IR. We have V = 18V and  $R = R_A = 25\Omega$  but we need to calculate the current through  $R_A$  first. So: **Step 1: Calculate the total resistance in the circuit:** 7.5 $\Omega$  is the total resistance between

Total resistance in the circuit =  $25\Omega + 7.5\Omega = 32.5\Omega$ Step 2: Calculate the current flowing through  $R_A$ : The current through  $R_A$  can be found using:

 $I = \frac{V_{total}}{R_{total}} = \frac{18 V}{32.5\Omega}$  $I = 0.5538 \dots A$ 

Step 3: Now you can use:  $V = IR_A = (0.5538 \dots A)(25\Omega)$ Therefore p.d. across  $R_A$  is 13.8V Always use the exact answer from your calculator until you get to the final answer and then you can round up or down to appropriate significant figures.

X and Y we

calculated in the

previous question.

#### c) Calculate the current in the $15\Omega$ resistor:

We know the current flowing into the group of three resistors and out of it, but not through the individual branches. But we know that their combined resistance is  $5\Omega$  (from part a) so you can work out the p.d. across the group:

$$V = IR = (0.5538 \dots A)(2.5\Omega) = \frac{18}{13}$$

The p.d. across the whole group is the same as the p.d. across each individual resistor, so you can use this to find the current through the  $7.5\Omega$ 

resistor:

$$I = \frac{V}{R} = \frac{\left(\frac{18}{13}V\right)}{7.5\Omega} = 0.1846 \dots A$$

So the current through the  $7.5\Omega$  resistor is 0.18A.

tutorpacks.co.uk

Χ

18V

2.5Ω

5Ω

## Please see '3.5.2 Series and Parallel Circuit worked examples' pack for exam style questions.

For more revision notes, tutorials and worked examples please visit www.tutorpacks.co.uk.

tutorpacks.co.uk

tutorpacks.co.uk

© Tutor Packs